

5. (2 pts each) Fill in the blank for the answers for the following limits based on the graph below. Each unit on the graph corresponds to one unit.

(a) $\lim_{x \rightarrow -1} f(x) =$

(b) $\lim_{x \rightarrow 10^-} f(x) =$

(c) $\lim_{x \rightarrow 17^+} f(x) =$

(d) $\lim_{x \rightarrow 4^+} f(x) =$

(e) $\lim_{x \rightarrow 10^+} f(x) =$

(f) $\lim_{x \rightarrow 17^-} f(x) =$

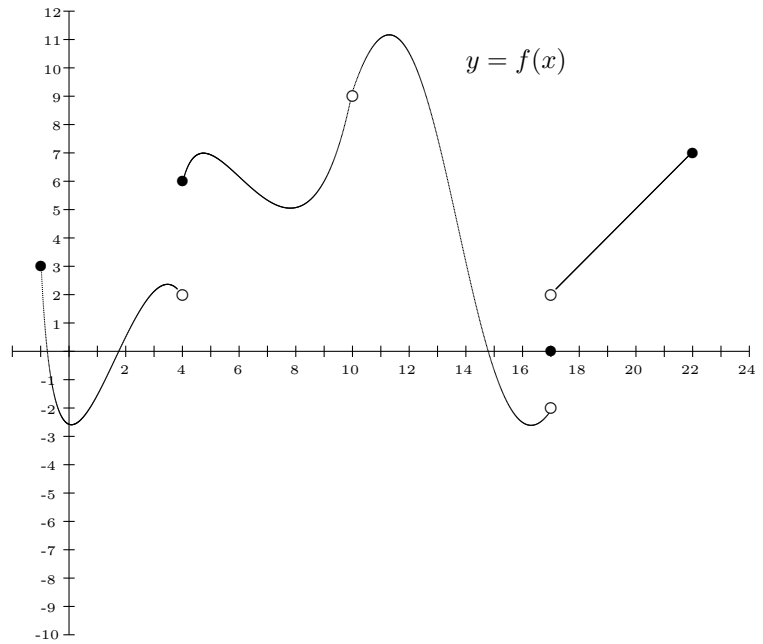
(g) $\lim_{x \rightarrow 10} f(x) =$

(h) $\lim_{x \rightarrow 4} f(x) =$

(i) $f(10) =$

(j) $f(4) =$

(k) $f(17) =$



- (l) At which points is $f(x)$ continuous?

- (m) At which points is $f(x)$ discontinuous?

- (n) At which points is $f(x)$ only right continuous?

- (o) At which points is $f(x)$ only left continuous?

Show Your Work

Show all work clearly and neatly. No work shown means no credit will be given. Use correct notation to get full credit. Reserve scratch paper work for scratch paper, which means only include necessary work on the exam. Erase all mistakes neatly. Keep it neat!

6. (5 pts) Find an equation for the circle with the center $(-1, 5)$ and radius $\sqrt{10}$.

7. (5 pts) Using the trigonometric identity $\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$, find $\cos\left(\frac{\pi}{12}\right)$. (Hint: $\frac{\pi}{12} = \frac{\pi}{3} - \frac{\pi}{4}$).

8. (5 pts) Calculate $\lim_{x \rightarrow 0^+} \frac{\sin x}{x}$ by using the sandwich theorem. (Hint: use the inequality that $x - \frac{x^2}{6} < \sin x < x$ for the interval $0 < x < \frac{\pi}{2}$).

9. (5 pts) Compute the following limit:

$$\lim_{x \rightarrow 2} \frac{\sqrt{x^2 + 12} - 4}{x - 2}$$

10. (5 pts) Calculate $\lim_{x \rightarrow -1^-} \left(\frac{x^2}{2} - \frac{1}{x} \right)$.

11. (5 pts) Show that $\lim_{x \rightarrow 0} \frac{\sin 5x}{\sin 4x} = \frac{5}{4}$.

12. (10 pts) Find the equation for the tangent line to the curve $f(x) = 4 - x^2$ at the point $(2, 3)$.

13. (7 pts) Compute the derivative of $f(x) = 2\sqrt{x}$ at the point $x = 4$.

14. (5 pts) Prove $\lim_{x \rightarrow -2} x^2 = 4$ by using the precise definition of the limit.